



# **Improved Structure for Three-Phase Four-Wires Hybrid Active Power Filters**

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**Abstract.** This paper presents a novel three-phase four-wire low power rating flexible hybrid active filter with a power factor, harmonic and neutral currents capability for distribution systems. The passive filter is tuned to compensate the two largest harmonics components and the power factor of the load. A selective algorithm is employed in order to enable the active filter to compensate only the desirable harmonic components. Simulation results are presented in order to verify the performance of the proposed hybrid filter.

# Key words

Harmonic compensation, Hybrid Active Filters, Power Quality, Reactive Power Compensation, Selective Algorithm.

# 1. Introduction

Regardless of the economic activities, all costumers depend, on some level, on electrical energy quality and network efficiency. Historically, the costumers were only interested in reduce their energy cost by compensating the reactive energy. However, with the increase of electricelectronics equipments in the distribution systems, nowadays the costumers are interested also in the electrical waveform quality in order to protect and guarantee a proper functioning of these sensitive loads. In fact, the improvement of power factor can release electrical capacity of the distribution system, improve the voltage level, reduce the system losses and optimize electrical energy costs. In this context, shunt capacitors have been installed in specific locations of the distribution feeders in order to compensate the reactive power. However, the widespread use of nonlinear loads can generate current harmonics and/or voltage harmonics that deteriorates the power quality of the distribution feeders and the application of shunt capacitors can lead to serious problems. Traditionally, in order to overcome the harmonic and reactive flow related problems, shunt passive filters have been adopted for a long time, but their practical applications provide limited solution to these power quality problems and have some disadvantages, such as large size equipments, fixed tuning and risk of resonance [1]. The series/parallel resonance may result in over-current/over-voltage and can damage the passive filter. Furthermore, the harmonics currents produced by

neighboring nonlinear loads may flow into the passive filter, resulting in overload situation.

The drawbacks of passive filters have increased the interest on active filtering applications. In this context, different topologies and control strategies of active power filters have been analyzed and discussed in the literature [2]. Due to this great interest in active filtering, some ideas emerged using the traditional passive filters combined with the active filters, resulting in the proposal of different hybrid filter topologies [3-5]. An effective hybrid active filter structure consists of active and passive resonant filter connected in series, which results in a lower required rated voltage source converter. Therefore, due to the low voltage level, the small shunt active filter can be connected in series with the shunt passive filter without using any coupling transformer. This hybrid active filter is characterized by a low dc-link rating with similar filtering performance with active power filters [6-9]. Some hybrid filter topologies coupling the voltage source converter to the distribution feeders trough series resonant filters have been presented for three-phase four-wire systems [9-13]. A classical topology based on three-phase three-leg converter with two split capacitors at the DC bus is showed in Figure 1.

Figure 2 shows a similar structure with a single capacitor at the DC bus and in this case the neutral wire is connected to negative point at the converter DC bus [11]. Another quite similar structure based on three-phase threeleg converter that uses a single capacitor at the DC bus is showed in Figure 3, which the negative point is connected to neutral wire by a specific inductor [10].



Fig. 1. Three-phase four-wire hybrid filter with split capacitor.



Fig. 2. Three-phase four-wire hybrid filter with asymmetric neutral connection.



Fig. 3. Three-phase four-wire hybrid filter with neutral inductor.

The neutral wire also can be connected directly in one leg of the converter. In this context, a classical topology based on three-phase four-leg converter is showed in Figure 4.



Fig. 4. Three-phase four-wire hybrid filter with four-leg converter.

In this work, the compensation performance of a new hybrid active power filter topology developed for threephase four-wire distribution system is presented and analyzed. This topology was based on hybrid active power filter topology presented in [12]. In the proposed topology the four-leg converter was is inserted between the capacitors and the two inductors groups of the shunt passive filter tuned for the  $5^{th}$  and  $3^{rd}$  harmonic order. This new configuration keeps the harmonic mitigation capability for a lower cost than the similar topology and presents more flexibility when the active filter is disconnected from the system. The paper shows that this proposed structure provides a reduction of inverter power rating by decreasing both its line current and line-to-line voltage. A preliminary analysis of the converter power losses also is discussed in this work.

### 2. Proposed Hybrid Filter Topology

The proposed three-phase four-wire hybrid active power filter topology is shown in Figure 5, which consists of a series connected two inductors and one capacitor set with a small-rating power converter. The structure of the proposed hybrid filter was based on the combination of the b-shaped one-branch and b-shaped L-type passive filters topologies, shown in Figure 6 [12] and Figure 7 [13-14], respectively.



Fig. 5. Three-phase four-wire proposed hybrid filter.



Fig. 6. Three-phase four-wire b-shaped L-Type hybrid filter.



Fig. 7. Three-phase four-wire b-shaped one-branch hybrid filter.

The passive filter structures of the proposed hybrid filter and the b-shaped L-type are similar. Both topologies have two set of inductors,  $L_1$ - $L_n$  and  $L_1$ - $L_2$ , respectively. However, the proposed topology has a single inductor installed in neutral of the system instead of three inductors in each phase, that present a resonant frequency for the zero sequence components. Meanwhile, the active filter connections of the proposed topology and the b-shaped one-branch are set between the capacitor and the inductor. However, the b-shaped one-branch structure has only one inductor per phase. In the original power circuit configurations, shown in Figure 6 and Figure 7, the passive filter can be keep the operating even when the active filter is disconnected. This is an important operational aspect for the reliability of distribution systems. However, in both topologies, only one resonance frequency can be obtained, usually the third harmonic.

In the proposed structure, with the active filter disconnected, the proposal topology has advantage in this operational situation because the passive filter can simultaneously drain the third and fifth harmonic components. On the other hand, the passive filter that composes the b-Shaped L-Type Hybrid Active Power Filter can drain only the third harmonic component in the same operational situation. This factor makes the proposal topology interesting by its reliability and greater operational flexibility

The b-shaped L-type topology presents a lower switching noise injection than the b-shaped one-branch topology due to the series connected inductor  $L_1$  and capacitor C that forms a  $L_1C$  filter as shown in Figure 6. However, this topology presents a higher cost and size [12]. The proposal topology presents lower cost and lower size than the b-shaped L-type topology but the switching noise injection is normally higher.

In the hybrid active filter shown in Figure 6, the tuning of the passive filter was defined to eliminate the two most dominant harmonics. The capacitance C and inductance  $L_1$  will be tuned at the second more dominant harmonic order and the set defined by C,  $L_1$  and  $L_2$  will be tuned at the first dominant harmonic order [12]. Thus, the passive filter will act in the two largest harmonics regardless of active filter. This assumption was maintained in the tuning of the proposed topology. However, if the passive filter C and L<sub>1</sub> would be tuned to 7<sup>th</sup> harmonic frequency, instead of the 5<sup>th</sup> harmonic order, the passive filter would be less bulky for the same filter capacitor C [16]. The choice to eliminate the 5<sup>th</sup> harmonic component was due to the fact that the passive filter can be operated itself. Thus, one can ensure the elimination of largest harmonics magnitudes with the active filter turn off.

The passive filter set of the proposed topology was tuning to presents a resonance frequency for positive and negative sequence components and zero sequence components [10].

The capacitor C and the inductor  $L_1$  forms a  $L_1C$  passive filter tuned to fifth harmonic component and the resonance frequency are given by (1)

$$f_5 = \frac{1}{2\pi\sqrt{L_1C}} \tag{1}$$

The capacitor C and both inductors  $L_1$  and  $L_n$  forms a  $L_{12}C$  passive filter tuned to third harmonic component and the resonance frequency is given by (2)

$$f_{3} = \frac{1}{2\pi \sqrt{(L_{1} + 3L_{n})C}}$$
(2)

In this proposal topology the passive filter presents an important characteristic to drain both harmonics currents components itself or in a combined operation with the active filter.

### 3. Control Strategy of the Active Filter

The main purpose of the control strategy of the active filter is to compensate the others harmonics presented in the distribution system not filtered by the passive filter. In distribution systems the larger harmonic components are, generally,  $3^{rd}$ ,  $5^{th}$ ,  $7^{th}$ ,  $9^{th}$ ,  $11^{th}$ ,  $13^{th}$ ,  $15^{th}$ ,  $17^{th}$  and  $19^{th}$ . In this case, the proposed passive filter is already set to compensate the  $3^{rd}$  and  $5^{th}$  harmonics components. Therefore, the control strategy of the active filter will be set to compensate the other harmonic components ( $7^{th}$ ,  $9^{th}$ ,  $11^{th}$ ,  $13^{th}$ ,  $15^{th}$ ,  $17^{th}$  and  $19^{th}$ ).

Furthermore, the reference currents, calculated through the control algorithm, are indirectly obtained from the system voltages [17]. This strategy guarantees that the proposed hybrid filter can operate independent of the power flow direction, for example, in a loop distribution system. The block diagram of the proposed control strategy for the active filter is presented in Figure 8.

As can be seen in Figure 8, the only input of the control strategy used to determine the reference currents of the active filter are the systems voltages ( $v_{Sa}$ ,  $v_{Sb}$ ,  $v_{Sc}$ ). The dc-link voltage ( $v_{dc}$ ) and the currents produced by the converter ( $i_{fa}$ ,  $i_{fb}$ ,  $i_{fc}$ ) inputs are used to regulate de dc-link capacitor voltage and current loop control, respectively.

The synchronizing circuit, presented in Fig. 9, is composed by a PLL (Phase Locked Loop) circuit, which is responsible to detect the frequency and phase angle of the fundamental positive sequence of the system voltage  $(v_{S\alpha'} \text{ and } v_{S\beta'})$  and generate the harmonic reference signals used in the detection circuit ( $v_{h\alpha}$  and  $v_{h\beta}$ ).

The detection circuit, responsible to extract the magnitude and phase of each harmonics components from the systems voltages, is presented in Figure 10. The concepts of the control algorithm are derived from the instantaneous power theory (pq-Theory) [18]. The harmonic components presented in the system voltages changes dynamically as the active filter compensates the harmonics component of the system currents.

Thus the power reference control algorithm, illustrated in Figure 11, uses a PI controller to determine dynamically the phase angle and magnitude of each harmonic component of the system voltages. Finally, the reference powers of each harmonic component  $(p_h^* \text{ and } q_h^*)$  are used in the pq-Theory to determine the harmonic currents  $(i_h^*)$  that have to be drained by the active filter.



Fig. 8. Block diagrams of the proposed control algorithm



Fig. 9. Synchronizing circuit.



Fig. 10. Detection circuit.



Fig. 11. Power reference circuit.

The dc-link and current loop control circuits present a usual algorithm and, therefore, they will be not presented in this paper.

### 4. System Modeling and Simulation Results

Figure 12 shows the power circuit of the proposal hybrid active power filter applied to a basic low voltage distribution system. This circuit was modeled, simulated and analyzed by means PSCAD/EMTDC environment.



Fig. 12. Power circuit of the distribution system and hybrid filter.

#### A. Power System Modeling

The medium voltage network was simplified using the sequence impedances representation at PCC. The positive and zero inductive reactance sequences were calculated using the information of the three-phase and single-phase short circuit capacity. The three-phase distribution transformer presents two winding 11.4 kV/220 V with a delta-star point grounded configuration, with a power rating equal to 75 kVA, and short circuit impedance (positive sequence leakage reactance) equal to 3.5 %. The neutral point of the low voltage side of the transformer is grounded by an 80  $\Omega$  resistor (R<sub>gnd</sub>). The low-voltage feeder was modeled by means coupled PI section with positive and zero sequence impedances representing a 53 mm aluminium cable with a distance of 30 meters. The load is composed by a linear load (RL) and nonlinear loads (three-phase and single-phase rectifiers), with an apparent power equal to 35 kVA with an inductive power factor equal to 0.82 and a current total harmonic distortion (THDi) of 14.8%.

#### B. Passive Filter Design

The filtering capacitance C was calculate for compensate the power factor of the load to, at least to 0.94 inductive. In this context, for this load scenario, it is necessary a 9.82 kVar capacitor bank. Therefore, a commercial capacitor bank of 10 kVAr / 220 V (capacitance value equal to 684.8 $\mu$ F/per phase) was chosen for the power factor correction. Now, with the filtering capacitance defined, (1) and (2) can be used in order to calculate de phase and the neutral inductors (L<sub>1</sub> and L<sub>n</sub>) to set the resonance frequencies of the passive filter to the 3<sup>rd</sup> and 5<sup>th</sup> harmonic. Table I summarize the system parameters for simulation.

#### C. Simulation Results

The power circuit was simulated with three different stages. The first one, the passive and the active filters were turned off  $(SW_{PF}$  and  $SW_{AF}$  open). At the second stage, only the passive filter is turned on  $(SW_{PF}$  closed and  $SW_{AF}$  open). At last, in the final stage, the active filter enters combined with the passive filter  $(SW_{PF}$  and  $SW_{AF}$  closed).

Table I Systems	Parameters	Simulation	Summary
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Parameters	Symbol	Value
Medium / Low voltages	$v_s$	11.4 /0.22 kV
Three-phase short circuit capacity	$L_s$	55 MVA
Single-phase short circuit capacity	Lo	18 MVA
Positive seq. leakage reactance	$X_{s}$	0.035 pu
Transformer no load losses	p <sub>no-load</sub>	0.0044 pu
Transformer copper losses	p <sub>copper</sub>	0.0153 pu
Positive sequence resistance 53mm AL	r <sub>+</sub>	0.6641 Ω/km
Zero seq.resistance 53mm AL	r <sub>o</sub>	1.7012 Ω/km
Positive seq inductive reactance 53mm AL	$\mathbf{X}_+$	0.1311 Ω/km
Zero seq.inductive reactance 53mm AL	Xo	1.0492 Ω/km
Filtering capacitance	С	684.8 μF
Filtering inductance	L	411 µH
Neutral filtering inductance	L <sub>n</sub>	244 µH
Inverter inductance	L <sub>c</sub>	250 µH
dc-link storage capacitance	C <sub>dc</sub>	2500 µF
Switching frequency	$f_s$	10 kHz

The instantaneous three-phase and neutral load currents before compensation are presented in Figure 13(a). In this case, with no compensation, the source current at the low voltage side of the transformer is the same of the load current. Figure 13(b) and (c) presents the source current ate the low voltage side of the transformer with only the filter and with the hybrid active filter passive compensation, respectively. The improvement of the current total harmonic distortion (THDi), observed in Figure 13(b), is possible only because the passive filter topology compensate, at the same time, the 3<sup>rd</sup> and 5<sup>th</sup> harmonics even without the active filter connected in to system. Furthermore, when the active filter is turned on, another improvement on the THDi was achieved. In this case, the active filter selective control algorithm compensates only the 7<sup>th</sup>, 11<sup>th</sup>, 13<sup>th</sup>, 15<sup>th</sup>, 17<sup>th</sup> and 19<sup>th</sup> harmonic components, optimizing the THDi.



Fig. 13. Source current (LV) without compensation (a), passive filter (b) and hybrid filter compensation (c).

The instantaneous phase voltage  $(v_{sa})$  and current  $(i_{sa})$  of the transformer low voltage side, without compensation and with the passive filter and hybrid active filter compensation, are presented in Figure 14(a), (b) and (c), respectively.

From Figure 14(b), the proposed passive filter can compensate the power factor of the distribution system and compensate the 3<sup>rd</sup> and 5<sup>th</sup> harmonics. Furthermore, it can be observed in Figure 14(c) that the active filter do not change the power factor of the distribution system. This is an important advantaged, because requires less current from the active filter, decreasing more the nominal power of the converter. However, if a power factor control circuit is needed, for example in a distribution system with a significant variation of the reactive power, the active filter can improve dynamically a percentage of the power factor. However, in this case, a current measurement will be necessary in order to calculate the power factor and more nominal power of the active filter will be needed. Since the purpose of this work is to reduce the rated power of the active filter, the reactive power control loop will be discarded.

Figure 15 presents the regulated dc-link capacitor voltage  $(v_{dc})$  and the rms current of the active filter for phase a  $(i_{AFa})$ . The dc capacitor was pre-charged to 65  $V_{dc}$  and at 3.3 seconds of simulation the active filter is connected into the system and the dc-link control algorithm is turned on.

The total rms current, for one phase of the converter, is 4.4 Arms. The rated power of the active filter was calculated through the output AC voltages and currents of the equipment. Therefore, the calculated rated power of the active filter was 300 W, proving the low rated power of the equipment.



Fig. 14 Source PF without (a) and with the passive filter (b).



Fig. 15 dc-link capacitor voltage and rms current of the active filter.

# 5. Conclusions and Future Works

In this paper was presented a new three-phase for-wire hybrid active filter structure enable to compensate reactive power, harmonics and neutral current. This hybrid active filter is characterized by operational flexibility and allows the simultaneous compensation of  $3^{rd}$  and  $5^{th}$  harmonics even without the connection of active filter. This factor makes the proposal topology interesting by its reliability and greater operational flexibility. Furthermore, the proposed active filter topology can reduce the nominal power rating of the active filter, without compromise the operational performance of the hybrid filter.

The simulations results prove the flexibility and viability of the proposed hybrid filter. The control algorithm of the hybrid active filter can extract the phase angle and magnitude of the selected harmonics by only monitoring the system voltages. This is an important advantage because guarantees that the proposed hybrid filter can operates independent of the power flow direction, for example, in a loop topology or in a radial topology with possibility of reconfiguration distribution systems.

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